

Time: 1 Hour

Full Marks: 20

The figures in the margin indicate full marks

Candidate are required to give their answer in their own words as far as practicable

Group A

Answer any 2 questions.

2x5

1. Given the following sets $A = \{a_1, a_2, a_3\}$, $B = \{b_1, b_2\}$, $C = \{c_1, c_2, c_3\}$

5

Fuzzy relation R is defined from A to B based on the following membership function:

$$\mu_R(a_i, b_j) = 1 - \frac{|i - j|}{3}$$

Fuzzy relation S is defined from B to C based on the following membership function:

$$\mu_S(b_j, c_k) = \frac{(j + k) \bmod 3}{2}$$

Using the max-min composition compute the fuzzy relation $R \circ S$.

2.

- a. A fuzzy control system outputs a fuzzy set defined on the universe of discourse $x \in [0,10]$. The fuzzy output set is given by the following membership function:

$$\mu(x) = \begin{cases} \frac{x}{5}, & 0 \leq x < 5 \\ \frac{10 - x}{5}, & 5 \leq x < 10 \\ 0, & \text{Otherwise} \end{cases}$$

This is a triangular fuzzy member with peak at $x = 5$ and height $\mu = 1$ forming a symmetric triangle from 0 to 10. compute the defuzzified crisp value of the output.

2

- b. Let fuzzy set A be defined over the universe $X = \{1,2\}$ with the membership function:

$$\mu_A = \{(1,0.3), (2,0.9)\}$$

Let fuzzy set B be defined over the universe $Y = \{a,b\}$ with the membership function:

$$\mu_B = \{(a,0.6), (b,1.0)\}$$

Assume the fuzzy universe Y is fully compatible, i.e.,

$$\mu_Y = \{(a,1.0), (b,1.0)\}$$

Using the fuzzy implication rule: $R = (A \times B) \cup (A' \times Y)$

Construct the fuzzy relation R representing the implication "If x is A, then y is B."

3

3. What is a fuzzy set? State any two differences between fuzzy logic and crisp logic. Give two simple real-life examples where fuzzy sets are used.

1 + 2 + 2

Group B

Answer any 2 questions.

2x5

- | | |
|--|-----|
| 4. Explain forward chaining with a suitable example. | 5 |
| 5. Convert the following sentences into First order predicate logic. | |
| i) All purple mushrooms are poisonous. | 1 |
| ii) Some boys like cricket. | 1 |
| iii) All Gorillas are black. | 1 |
| iv) Some cats are intelligent. | 1 |
| v) Everyone likes Ram. | 1 |
| 6. Explain alpha-beta pruning with an example. | 5 |
| 7. What is resolution? Explain with an example. | 2+3 |

-----X-----